

Code: EE4T1

**II B.Tech - II Semester – Regular/Supplementary Examinations –  
April 2019**

**COMPLEX VARIABLES & SPECIAL FUNCTIONS  
(ELECTRICAL & ELECTRONICS ENGINEERING)**

Duration: 3 hours

Max. Marks: 70

PART – A

Answer *all* the questions. All questions carry equal marks

11 x 2 = 22 M

1.

- a) Find the real and imaginary parts of  $\text{Cosh}(x+iy)$ .
- b) Find all the roots of the equation:  $\text{Sin}z = \text{Cosh}4$ .
- c) List the C-R equations in polar co-ordinates.
- d) State Cauchy's integral formula.
- e) Define Complex potential Function.
- f) Determine the poles of the function  $f(z) = \frac{1-e^{2z}}{z^4}$ .
- g) Find the poles and residues at each pole of  $\tanh z$ ?
- h) Find the image of the infinite strip  $0 < y < \frac{1}{2}$  under the transformation  $w = \frac{1}{z}$ .
- i) Find the bilinear transformation which maps the points  $(-1, 0, 1)$  into the points  $(0, i, 3i)$
- j) Determine  $\frac{d}{dx} J_0(x)$ .
- k) Express the function in Legendre polynomial  $5x^3+x$

PART – B

Answer any **THREE** questions. All questions carry equal marks.

3 x 16 = 48 M

2. a) Show that the function  $f(x,y) = x^3y - xy^3 + xy + x + y$  can be imaginary part of an analytic function  $z = x + i y$ .

8 M

- b) Find  $f(z) = u + iv$  given that  $u + v = \frac{\sin 2x}{\cosh 2y - \cos 2x}$ .

8 M

3. a) Evaluate  $\int_C (x - 2y)dx + (y^2 - x^2)dy$  Where C is the boundary of the first quadrant of the Circle  $x^2 + y^2 = 4$ .

8 M

- b) Develop  $f(z) = \frac{1 + 2z}{z^2 + z^3}$  in a series of positive and negative powers of z.

8 M

4. a) Evaluate  $\int_C \frac{\sin^6 z}{(z - \frac{\pi}{6})^3} dz$  where C:  $|z| = 1$ .

8 M

- b) Evaluate  $\int_0^{2\pi} \frac{d\theta}{(5 - \cos \theta)^2}$  using residue theorem.

8 M

5. a) Show that circles are invariant under linear and inversion transformations.

8 M

b) Find the bilinear transformation which maps the points

$z=1, i, -1$  onto the points  $w=i, 0, -i$  hence find

i) the image of  $|z| < 1$

ii) the invariant points of this transformation.

8 M

6. a) State and prove the Orthogonality of the Bessel's function.

8 M

b) Prove that:  $P_n(x) = \frac{1}{n!2^n} \frac{d^n}{dx^n} (x^2 - 1)^n$ .

8 M